

Precalculus – Exam 5 Review

Use identities to simplify each expression:

1. $\frac{\tan x \csc x}{\sec x}$

2. $\tan^2 x - \frac{\sin(-x)}{\sin x}$

3. $\frac{\cos^2 x - \sin^2 x}{2 \sin x \cos x}$

4. $\frac{1}{1 + \sin \alpha} + \frac{\sin \alpha}{\cos^2 \alpha}$

5. $\frac{2 \tan(2\theta)}{1 - \tan^2 2\theta}$

6. $\sin \theta \cos \theta (\tan \theta + \cot \theta)$

7. $\sin^2 x \tan^2 x + \sin^2 x$

8. $\cos 75^\circ \cos 60^\circ + \sin(-75^\circ) \sin 60^\circ$

9. $\sin 80^\circ \cos(-50^\circ) - \sin 10^\circ \sin 50^\circ$

10. $\frac{\sin(4y)}{1 + \cos(4y)}$

Verify each identity:

$$11. \frac{\sin x \cos x}{\tan x} = 1 - \sin^2 x$$

$$12. \cot(-y) = \frac{1 - \sin^2 y}{\cos(-y) \sin(-y)}$$

$$13. \frac{\sin 2\beta}{2 \csc \beta} = \sin^2 \beta \cos \beta$$

$$14. \frac{1}{\sec \theta - 1} - \frac{1}{\sec \theta + 1} = 2 \cot^2 \theta$$

$$15. \cos(3x) = \cos x(1 - 4 \sin^2 x)$$

$$16. \sin^2\left(\frac{x}{2}\right) = \frac{\csc^2 x - \cot^2 x}{2 \csc^2 x + 2 \csc x \cot x}$$

$$17. \frac{\sin(2\alpha)}{1 + \cos(2\alpha)} = \tan(\alpha)$$

$$18. \sec(2\theta) = \frac{1 + \tan^2 \theta}{1 - \tan^2 \theta}$$

Find the exact value by using a sum or difference identity:

19. $\cos\left(\frac{7\pi}{12}\right)$

20. $\sin\left(-\frac{5\pi}{12}\right)$

21. $\tan 195^\circ$

Find the exact value by using a half-angle identity.

22. $\sin\left(-\frac{\pi}{8}\right)$

23. $\cos 75^\circ$

24. $\tan\left(\frac{5\pi}{8}\right)$

Use the given information to find the exact value of the trigonometric function(s).

25. Find $\sin(A+B)$ if $\sin A = -5/13$ and $\cos B = 3/5$, with A in quadrant III and B in quadrant I.

Use the given information to find the exact value of the trigonometric function(s).

26. Find $\cos(\alpha + \beta)$ if $\sin \alpha = 15/17$ and $\sin \beta = -1/3$, with α in quadrant II and β in quadrant IV.

27. Find $\cos \alpha/2$ if $\sin \alpha = -1/4$, and α is in quadrant IV.

28. Find $\sin 2\theta$ if $\cos \theta = -12/13$, and θ is in quadrant II.

29. Find $\sin \beta$, $\cos \beta$, and $\tan \beta$ if $\cos(2\beta) = 24/25$ and $180^\circ < 2\beta < 360^\circ$.

30. Find $\sin \alpha$, $\cos \alpha$, and $\tan \alpha$ if $\sin(\alpha/2) = -2/7$ and $\pi < \alpha/2 < 5\pi/4$.