

# Analyzing Functions Study Guide

## Domain and Range:

- **Domain:** all  $x$ -coordinates on the graph from *left to right*.
- **Range:** all  $y$ -coordinates on the graph from *bottom to top*.
  - Graphs with unconnected dots (no solid line): List  $x$ 's and  $y$ 's in { and }.
    - Don't list repeated numbers more than once.
  - Graphs with solid lines (even if there are labeled dots on it):
    - Use interval notation:  $(\_, \_)$ ,  $(\_, \_]$ ,  $[\_, \_)$ , or  $[\_, \_]$ .
    - If there's an arrow on the end of a graph, the domain and range will involve  $-\infty$  or  $\infty$ .
    - Use [ or ] for endpoints and vertices (places where the graph changes direction).
    - Use ( or ) for  $-\infty$ ,  $\infty$ , asymptotes, or open circles.

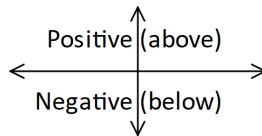
## Increasing, Decreasing or Constant: (Write $x$ 's)

- Write  $x$ -coordinates where graph starts and stops going each direction from *left to right*.
- Always use ( and ).
- **Increasing:** Uphill from left to right.
- **Decreasing:** Downhill from left to right.
- **Constant:** Flat.
- **Hint:** Look for places where the graph changes direction (relative maxima or relative minima) to help you break the graph into intervals.
- Use the  $\cup$  sign to connect multiple intervals:  $(\_, \_) \cup (\_, \_)$



## Positive or Negative: (Write $x$ 's)

- **Positive:** Above  $x$ -axis.
- **Negative:** Below  $x$ -axis.
- Divide the graph into the parts that are above the  $x$ -axis and the parts that are below the  $x$ -axis using the  $x$ -intercepts. Write  $x$ -coordinates for the *start* and *end* of each interval from *left to right*.
- Use ( and ) at  $x$ -intercepts.
- Use [ or ] only when there is an endpoint above or below the  $x$ -axis.
- Use the  $\cup$  sign to connect multiple intervals:  $(\_, \_) \cup (\_, \_)$



## Intercepts: The points where the graph crosses the $x$ - or $y$ -axis.

- Write intercepts as ordered pairs.
  - $x$ -intercepts are written as  $(x, 0)$ .
  - $y$ -intercepts are written as  $(0, y)$ .
- To find  **$x$ -intercepts** algebraically, set  $y = 0$  and solve for  $x$ .
- To find  **$y$ -intercepts** algebraically, set  $x = 0$  and solve for  $y$ .

## Relative Maximum or Relative Minimum:

- **Relative maximum:** a point on the graph that is **higher** than all the points around it.
- **Relative minimum:** a point on the graph that is **lower** than all the points around it.
- **Maximum or minimum point:** Write ordered pair:  $(x, y)$ .
- **Maximum or minimum value:** Write  **$y$ -coordinate** of the point.

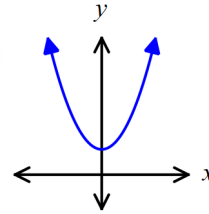
**End Behavior:** End behavior describes what is happening to the **y-coordinates** of the graph as you move left ( $x \rightarrow -\infty$ ) or as you move right ( $x \rightarrow \infty$ ).

- **Left end behavior** looks like this:  $\lim_{x \rightarrow -\infty} f(x) = \underline{\hspace{1cm}}$ .
- **Right end behavior** looks like this:  $\lim_{x \rightarrow \infty} f(x) = \underline{\hspace{1cm}}$ .
- **Arrow pointing up:** Write  $\infty$
- **Arrow pointing down:** Write  $-\infty$
- **Endpoint (no arrow):** Write D.N.E. (does not exist)
- **Asymptote or flat end with arrow:** Write y-coordinate of asymptote or flat part

**Symmetry:**

- **Even symmetry (y-axis):**
  - The left and right sides are mirror images around the y-axis. (Left and right sides would overlap if you fold the graph along the y-axis).

**Even:**



- **Odd symmetry (origin):**
  - If you fold the graph along the x-axis and then along the y-axis, the two halves will overlap.
  - If you spin the graph around  $180^\circ$ , you will end up with what you started with.

**Odd:**

