

Precalculus: 5.4 Homework Odd Answers

1. 1

3. $-\frac{1}{2}$

5. $\sin(26)$

7. $\frac{1}{\sqrt{3}}$

9. $\frac{\sqrt{2+\sqrt{2}}}{2}$

11. $2+\sqrt{3}$

13. $-\frac{\sqrt{2-\sqrt{3}}}{2}$

15. $-\frac{1}{2}$

17. $\cos\left(\frac{2\pi}{9}\right)$

19. Hint: Draw a triangle for 2α to find $\cos(2\alpha)$, then use an identity to find $\cos(\alpha)$, then draw another triangle for α .

$$\cos \alpha = -1/\sqrt{17}$$

$$\sec \alpha = -\sqrt{17}$$

$$\sin \alpha = 4/\sqrt{17}$$

$$\csc \alpha = \sqrt{17}/4$$

$$\tan \alpha = -4$$

$$\cot \alpha = -1/4$$

21. $\cos \alpha = -7/8$

$$\sec \alpha = -8/7$$

23. $-\frac{161}{289}$

$$\sin \alpha = -\sqrt{15}/8$$

$$\csc \alpha = -8/\sqrt{15}$$

$$\tan \alpha = \sqrt{15}/7$$

$$\cot \alpha = 7/\sqrt{15}$$

25. $\cos^4 \theta - \sin^4 \theta = (\cos^2 \theta + \sin^2 \theta)(\cos^2 \theta - \sin^2 \theta)$

$$= (1)(\cos(2\theta))$$

$$= \cos(2\theta)$$

27.

$$\begin{aligned} \frac{\cos(2x) + \cos(2y)}{\sin x + \cos y} &= \frac{1 - 2\sin^2 x + 2\cos^2 y - 1}{\sin x + \cos y} \\ &= \frac{2\cos^2 y - 2\sin^2 x}{\sin x + \cos y} \\ &= \frac{2(\cos^2 y - \sin^2 x)}{\sin x + \cos y} \\ &= \frac{2(\cos y + \sin x)(\cos y - \sin x)}{\cos y + \sin x} \\ &= 2(\cos y - \sin x) \\ &= 2\cos y - 2\sin x \end{aligned}$$

29. $\frac{\cos(2x)}{\sin^2 x} = \frac{1 - 2\sin^2 x}{\sin^2 x}$

$$\begin{aligned} &= \frac{1}{\sin^2 x} - \frac{2\sin^2 x}{\sin^2 x} \\ &= \csc^2 x - 2 \end{aligned}$$