

**Precalculus**  
**5.1 Homework**

**Write each expression in terms of sines and/or cosines, and then simplify.**

1.  $\frac{\cot x}{\csc x}$

2.  $\frac{\sin x}{\csc x} + \frac{\cos x}{\sec x}$

3.  $\frac{1}{\sin^2 x} - \frac{1}{\tan^2 x}$

4.  $\frac{1 + \cos \beta \tan \beta \csc \beta}{\csc \beta}$

5.  $\frac{(\cos \alpha \tan \alpha + 1)(\sin \alpha - 1)}{\cos^2 \alpha}$

**Use identities to find the exact values of the five remaining trigonometric functions at  $\alpha$ .**

6.  $\sin \alpha = 3/4$  and  $\pi/2 < \alpha < \pi$

7.  $\cot \alpha = -1/3$  and  $-\pi/2 < \alpha < 0$

8.  $\sec \alpha = -4\sqrt{5}/5$  and  $\alpha$  is in quadrant III

**Multiply.**

$$9. (2 \tan \alpha + 1)(2 \tan \alpha - 1)$$

$$10. (3 \sin \theta + 2)^2$$

$$11. (2 \cos \beta + 1)(\cos \beta - 1)$$

**Factor completely.**

$$12. \tan^2 \alpha - \sec^2 \beta$$

$$13. \csc^4 x - \csc^2 x$$

$$14. \sin^2 \theta \cos \theta + \sin \theta \cos \theta - 2 \cos \theta$$

$$15. 2 \sin^2 x - 5 \sin x - 3$$

**Simplify each expression.**

$$16. \sin(-x) \cot(-x)$$

$$17. \cos(y) + \cos(-y)$$

$$18. \frac{\sin(x)}{\cos(-x)} - \frac{\sin(-x)}{\cos x}$$

$$19. (1 + \sin(\alpha))(1 + \sin(-\alpha))$$

$$20. \sin \beta \cos(-\beta) \csc(-\beta)$$

$$21. 1 - \frac{1}{\cos^2 x}$$

$$22. \frac{\sin^2 \alpha - \cos^2 \alpha}{1 - 2 \cos^2 \alpha}$$

$$23. 1 - \frac{\sec^2 x}{\tan^2 x}$$

$$24. \sin x + \frac{\cos^2 x}{\sin x}$$

$$25. \frac{\sin^4 x - \sin^2 x}{\sec x}$$