

Precalculus

10.3 Odd Answers

$$\begin{aligned} 1. \quad a_n &= -2n^2 \\ a_{n-1} &= -2(n-1)^2 \\ &= -2(n^2 - 2n + 1) \\ &= -2n^2 + 4n - 2 \end{aligned}$$

NEITHER

$$\begin{aligned} \text{Arithmetic? } a_n - a_{n-1} &= (-2n^2) - (-2n^2 + 4n - 2) \\ &= -2n^2 + 2n^2 - 4n + 2 \\ &= -4n + 2 \\ &\text{Not constant, so not arithmetic} \end{aligned}$$

$$\begin{aligned} \text{Geometric? } \frac{a_n}{a_{n-1}} &= \frac{-2n^2}{-2(n-1)^2} = \frac{n^2}{(n-1)^2} \\ &\text{Not constant, so not geometric} \end{aligned}$$

$$\begin{aligned} 3. \quad a_n &= 3 - 5n \\ a_{n-1} &= 3 - 5(n-1) \\ &= 3 - 5n + 5 \\ &= 8 - 5n \end{aligned}$$

$$\begin{aligned} \text{Arithmetic? } a_n - a_{n-1} &= (3 - 5n) - (8 - 5n) \\ &= 3 - 5n - 8 + 5n \\ &= -5 \\ &\text{Constant, so ARITHMETIC!} \end{aligned}$$

$$5. \quad a_n = 12 \left(\frac{1}{4} \right)^{n-1}; \quad a_5 = \frac{3}{64}$$

$$7. \quad \frac{1}{64}$$

$$9. \quad 768$$

$$11. \quad a_n = -(-3)^{n-1}$$

$$13. \quad \frac{349,524}{5} \text{ or } 69,904.8$$

$$15. \quad 7,324,218$$

$$17. \quad 4.199947\dots$$

$$19. \quad \text{diverges}$$

$$21. \quad \text{converges; } 12$$

$$23. \quad \text{converges; } -\frac{20}{7}$$

$$25. \quad 1.8447 \times 10^{19} \text{ grains}$$